

U3

Adversarial Search & Games.

Page No.

Date

- # Adversarial Search Problem:- having competitive activity involving 'n' players & follows protocols.
- adversarial Games:- agents with conflicting goals.
- dealing with a competitive multi agent environment.
 - many unpredictable moves / actions.
 - Analyze & strategize.

Environment types.

- ① competitive - every agent makes effort to win
- ② Cooperative - agents jointly perform activity

Zero Sum Game

player 1 win = +1 } sum = 0
 player 2 loss = -1 } (+1, -1, 0 are called payoffs)

Non-Zero Sum Game

player 1 wins does not necessarily mean player 2 lost.

- ① Positive Sum game: Cooperative (all have same goal)
- ② Negative Sum game: Competitive (no one wins eg WAR)

Relevant aspects of Game

- ① Accessible env:- Game with accessible env have all info at hand
- ② Search:- games requiring search possible game positions to play game
- ③ Unpredictable opponent:- introduces uncertainty in the game

Game Theory:-

Branch of Maths & AI that studies interaction among rational agents. Where the outcome of is dependent on not only on their own actions but also on action of

others.

- used in AI for decision making, strategy formulation & modeling competitive & cooperative behaviour among agents.

Stochastic Game

- ① Outcome influenced by random events.
- ② includes probabilistic state transitions.
- ③ ~~fully~~ fully observable env
- ④ Eg:- Ludo
- ⑤ Key technique used.
MDP, RL Learning

Partial Game

- ① A game where players have incomplete or limited info
- ② Not necessarily random.
- ③ partially observable env
- ④ Eg. poker, card game
- ⑤ key techniques used
PO MDP

Types of Game strategies

- ① Equalizing strategy - produces same avg winning
- ② Optimal strategy - min max strategy.
- ③ pure & mixed strategies - pure \rightarrow easy stats. mixed \rightarrow complex stats.

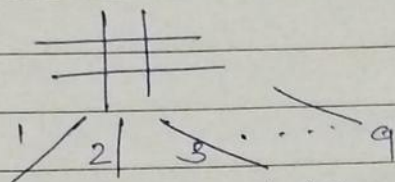
Types of Games.

- ① Deterministic \rightarrow fully observable env
- ② Non Deterministic
- ③ perfect info.
- ④ ~~Non~~ perfect info
- ⑤ Zero sum game
- ⑥ non zero sum game
- ⑦ constant sum game
- ⑧ n person game

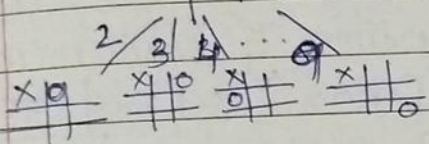
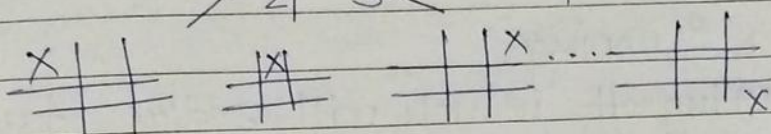
Game tree

- directed graph with nodes & edges.
- nodes \rightarrow position in game.
- edges \rightarrow next action.

eg.



* initial move is always indicated with max to win (max chance)



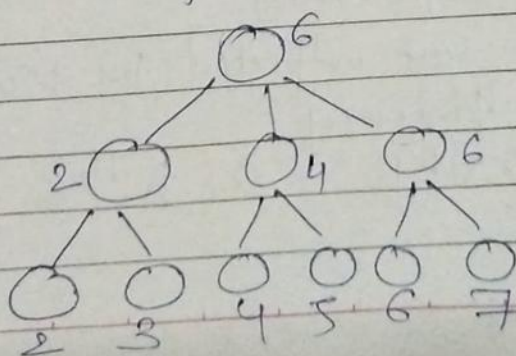
MinMax Algo.

- evaluates decision based on present state of game
- needs deterministic env with perfect info.
- based on the successor state every time the min max value is calculated. (by recursive computation)
- the selected value, with highest minMax value should be equal to the best possible outcome against best play.

Steps.

- ① create a game tree
- ② Assign val. to terminals / leaf nodes.
- ③ apply Min & Max opp. alternately & propagate upwards
- ④ find max for root. end.

can be done like
leaf node 0/1 for
loss/win



max

min

max Terminal

properties of MinMax Algo.

- ① Complete if tree is finite.
- ② Optimal if limited opponents.
- ③ Time complexity $O(b^d)$ \Leftarrow Space same.
- ④ uses DFS.

== Alpha Beta Pruning.

pruning:- cutting off. which will reduce tree size & help in reducing processing time & save memory

$\alpha \Rightarrow$ best choice, highest val (max) set to $-\infty$

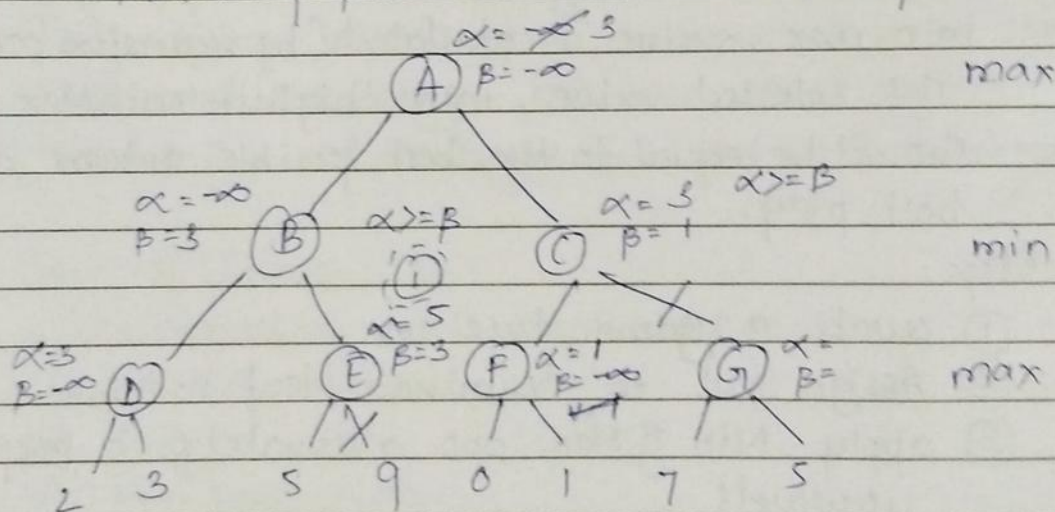
$\beta \Rightarrow$ lowest val along the path of minimizer. $+\infty$

condition $\alpha \geq \beta$

max update α val. | min updates β .

- node val passed to upper nodes.

- α, β only passed to child node not upwards.



== properties of α - β pruning

- ① final result not affected by pruning
- ② improved efficiency
- ③ time complexity $O(b^{d/2})$

→ try to find best part

Monte Carlo tree Search

- MCTS is a heuristic search algo used for decision making
- useful in large game trees (traditional game search not possible)
 - builds search tree ~~exp~~ asymmetrically
 - focus on promising moves by running simulations.

Steps.

① Selection.

- Start at root, select child based on ^{selection} policy like UCT
- move down until u reach a node that is not fully expanded.

② Expansion.

- add child node to tree by exploring one or more untried moves from selected node

③ Simulation.

- simulate a game till the end using random or semi-random moves

④ Back propagation.

- propagate the result (win/loss/draw) & repeat.

eg.

X	O
	X
O	

⇒

①

X	O
	X
O	X

②

X	O
	X
O	X

propagate

propagate loss.

propagate win

Adv. ① works well with large spaces

② No need of complete evaluation func.

③ Search focused on promising node

Application ① games like chess.

② AI agent is planning & Robotic.

- [#] Node Consistency:- A single variable is node consistent if all the values in the variable domain satisfy the variable's unary constraint. (for single var)
- [#] Path consistency (A, B has consistent assignment) C doesn't disrupt that & have an assignment.

Constraint Satisfaction problem

- process of finding a sol to a set of constraints
- finding a group of variables that fulfill a set of restrictions or rules. \leftarrow AIM
- Components of CSP
 - ① Variables \rightarrow fields to cover. (work on this part is done)
 - ② Domain \rightarrow possible values.
 - ③ Constraints. - a pair of scope + relation

Scope \Rightarrow variables that participate in constraint relation \Rightarrow list of valid value combinations.

- backtracking used if stuck in a problem due to constraints

Eg \rightarrow Variables \rightarrow WT, NT, SA, Q, NS, V, T

Domains \rightarrow R, G, B.

Constraints \rightarrow

WT \neq (NT, SA)

SA \neq NT, Q, NS, V

NT \neq Q

N \neq V

T

WT	NT	Q
	SA	NS
		V

Domain	WT	NT	SA	Q	NS	V	T
Initial Domain	RGB	RGB	RGB	RGB	RGB	RGB	RGB
R	R	GB	GB	RGB	RGB	RGB	RGB
G	R	G	B	R	RG	RG	RGB
B	R	G	B	R	RG	RG	RGB
R	R	G	B	R	RG	RG	RGB
R	R	G	B	R	R	G	R
G	R	G	B	R	R	G	R

- if trapped back track & change color.

Arc consistency:- A value is in Arc consistent ~~if~~ with other var.
 if for every var in its domain, there is one value in the other variables domain that satisfies the binary constraints between them.
 binary constraints:- rule involving 2 variables

Page No.

Date

CRYPTO Arithmetic.

x_3, x_2, x_1
 $6T \quad W^3 \quad 04$
 $6T \quad W^3 \quad 04$

 $F \quad 0 \quad U \quad R$
 $2 \quad 2 \quad 6 \quad 8$

$0 \rightarrow F, X, R$
 2
 $3 \leftarrow W.$
 $4 \rightarrow 4$
 $5 \leftarrow 0.$
 $6 \leftarrow 0$
 $7 \leftarrow W.$
 8
 9

$$20 = R$$

$$2T = 0$$

$$2W = U$$

(1) consider leftmost as 1.

(2) take rightmost value small as possible.

(3) R to L

~~9~~ 8 5 N 6 7
~~1~~ M 0 0 R 8 E 5
~~1~~ 0 N E 2
~~6~~ 5

$0 \leftarrow 00$
 $1 \leftarrow M$
 $2 \leftarrow R$
 3
 $4 \leftarrow E$
 $5 \leftarrow E$
 $6 \leftarrow N$
 $7 \leftarrow D$
 8
 $9 \leftarrow 85$

~~5~~ ~~6~~ ~~7~~

$$E + 0 = N$$

$$0 = N - E + 1$$

Note:- $7 \neq 6 = 13$

(1)

$$\begin{array}{r}
 N \quad 7 \\
 + R \quad 8 \\
 \hline
 E \quad 5
 \end{array}$$

E only = 5 not 15

Constraint propagation

/ legal values

- narrowing down possible domain values for a variable (step by step).

- communicating domain (reduced) for further variables.

- This process results in more domain reductions.

- domain reductions are propagated to appropriate constraints.

Adv.

(1) reduce search space by pruning dead end branches

(2) reveal hidden structures & symmetries in problem in early constraint propagation

Local consistency :-

- used to reduce no. of possible values by checking if they work with their immediate neighbors.